



# Cambridge International AS & A Level

CANDIDATE  
NAME

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CENTRE  
NUMBER

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## FURTHER MATHEMATICS

9231/13

Paper 1 Further Pure Mathematics 1

May/June 2021

2 hours

You must answer on the question paper.

You will need: List of formulae (MF19)

### INSTRUCTIONS

- Answer **all** questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do **not** use an erasable pen or correction fluid.
- Do **not** write on any bar codes.
- If additional space is needed, you should use the lined page at the end of this booklet; the question number or numbers must be clearly shown.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.

### INFORMATION

- The total mark for this paper is 75.
- The number of marks for each question or part question is shown in brackets [ ].

This document has **20** pages. Any blank pages are indicated.





2 The cubic equation  $2x^3 - 4x^2 + 3 = 0$  has roots  $\alpha, \beta, \gamma$ . Let  $S_n = \alpha^n + \beta^n + \gamma^n$ .

(a) State the value of  $S_1$  and find the value of  $S_2$ . [3]

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(b) (i) Express  $S_{n+3}$  in terms of  $S_{n+2}$  and  $S_n$ . [1]

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(ii) Hence, or otherwise, find the value of  $S_4$ . [2]

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4 The matrices **A**, **B** and **C** are given by

$$\mathbf{A} = \begin{pmatrix} 2 & k & k \\ 5 & -1 & 3 \\ 1 & 0 & 1 \end{pmatrix}, \quad \mathbf{B} = \begin{pmatrix} 1 & 0 \\ 0 & 1 \\ 1 & 0 \end{pmatrix} \text{ and } \mathbf{C} = \begin{pmatrix} 0 & 1 & 1 \\ -1 & 2 & 0 \end{pmatrix},$$

where  $k$  is a real constant.

(a) Find **CAB**.

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(b) Given that **A** is singular, find the value of  $k$ .

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(c) Sketch  $C$ , stating the coordinates of the intersections with the axes.

[3]

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(d) Sketch the curve with equation  $y = \left| \frac{x^2 - x - 3}{1 + x - x^2} \right|$  and find in exact form the set of values of  $x$  for which  $\left| \frac{x^2 - x - 3}{1 + x - x^2} \right| < 3$ .

[6]



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